



#### Physics 2102

#### **Magnetic fields**



# Question

Two charged ions A and B traveling with a constant velocity **v** enter a box in which there is a <u>uniform</u> magnetic field directed out of the page. The subsequent paths are as shown. What can you conclude?

- (a) Both ions are negatively charged.
- (b) Ion A has a larger mass than B.
- (c) Ion A has a larger charge than B.
- (d) None of the above.

#### (a) F=qv x B.

The vector v x B will point down when the charges enter the box; the force also points down for cw motion: charges must be positive. (b,c) r = mv/qB

Same speed and B for both masses; larger radius for A than B. Ion with larger mass/charge ratio (m/q) moves in circle of larger radius. But that's all we know! We cannot conclude b or c.

(d) Is the right answer.



 $F_B = q v x B$ 

 $r = \frac{mv}{qB}$ 

### **Crossed fields**

The figure shows four directions for the velocity vector v of a positively charged particle moving through a uniform electric field E (out of the page) and a uniform magnetic field B.

• Rank directions 1, 2, 3 according to the magnitude of the net force on the particle.

• If the net force is zero, what is the direction and magnitude of the particle's velocity?



#### Electric and magnetic forces: example



A solid metal cube moves with constant velocity v in the ydirection. There is a uniform magnetic field B in the zdirection.

- a) What is the direction of the magnetic force on the electrons in the cube?
- b) What is the direction of the electric field established by the electrons that moved due to the magnetic force?
- c) Which cube face is at a lower electric potential due to the motion through the field?
- d) What is the direction of the electric force on the electrons inside the cube?
- e) If there is a balance between electric and magnetic forces, what is the potential difference between the cube faces (in terms of the cube's velocity v, side length d and magnetic field B)?



http://en.wikipedia.org/wiki/Comparison\_of\_display\_technology

**Magnetic force on a wire** 



Note: If wire is not straight, compute force on differential elements and integrate:

$$d\vec{F} = i \, d\vec{L} \times \vec{B}$$

## The Rail Gun

- Conducting projectile of length 2cm, mass 1g carries constant current 10A between two rails.
- Magnetic field B = 1T points outward.
- Assuming the projectile starts from rest at t = 0, what is its speed after a time t = 1s?
  - Force on projectile = *i*LB
  - Acceleration = iLB/m
  - v(t) = iLBt/m
    - = (10A)(0.02m)(1T)(1s)/(0.001kg)
    - $= 200 \text{ m/s} \sim 450 \text{ mph}$

But:  $d=0.5(iLB/m)t^2 = 0.5 v(t) t = 100 m!!$ 



(from  $\mathbf{F} = i\mathbf{L} \ge \mathbf{B}$ ) (from F = ma) (from  $v = v_0 + at$ )

### Rail guns in the "Eraser" movie

"Rail guns are hyper-velocity weapons that shoot aluminum or clay rounds at just below the speed of light. In our film, we've taken existing stealth technology one step further and given them an X-ray scope sighting system," notes director Russell. "These guns represent a whole new technology in weaponry that is still in its infancy, though a large-scale version exists in limited numbers on

battleships and tanks. They have incredible range. They can pierce three-foot thick cement walls and then knock a canary off a tin can with absolute accuracy. In our film, one contractor has finally developed an assault-sized rail gun. We researched this quite a bit, and the technology is really just around the corner, which is one of the exciting parts of the story."



*Warner Bros., production notes, 1996. http://movies.warnerbros.com/eraser/cmp/prodnotes.html#tech* 

#### Also: INSULTINGLY STUPID MOVIE PHYSICS: http://www.intuitor.com/moviephysics/