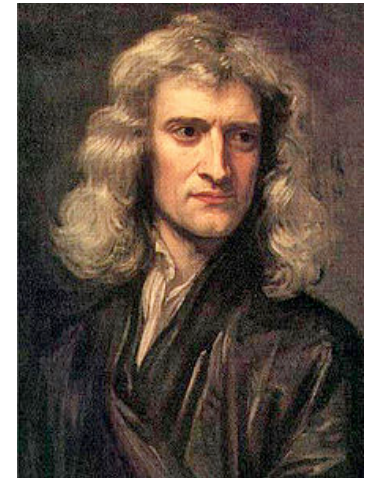
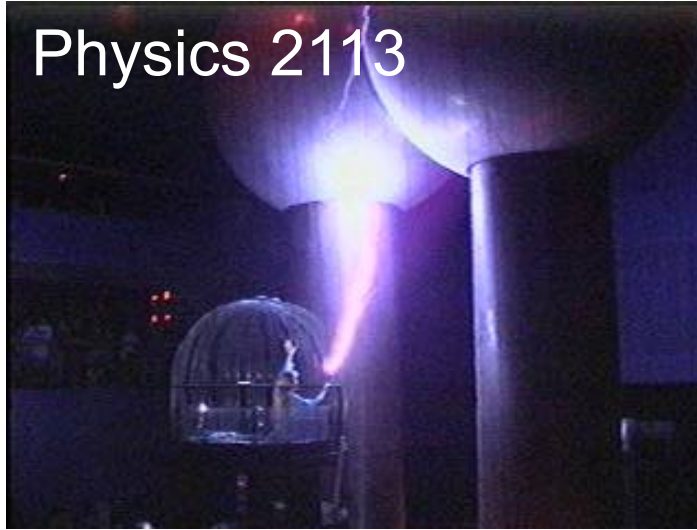


Physics 2113



Isaac Newton  
(1642–1727)

# Physics 2113

## Lecture 04: WED AUG 3

### CH21: Electric Charge



21-2	Electric Charge	561
21-3	Conductors and Insulators	563
21-4	Coulomb's Law	565



Michael Faraday  
(1791–1867)

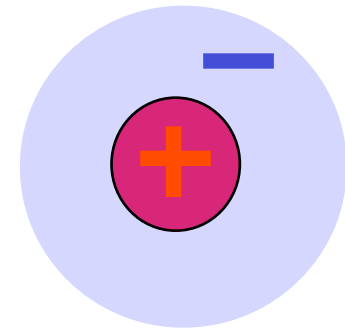
# Electric charges

- Two types of charges: positive/negative
- **Like** charges **repel**
- **Opposite** charges **attract**

## Atomic structure :

- negative electron cloud
- nucleus of positive protons, uncharged neutrons

*[[Why doesn't the nucleus fly apart??  
Why doesn't the atom collapse??]]*

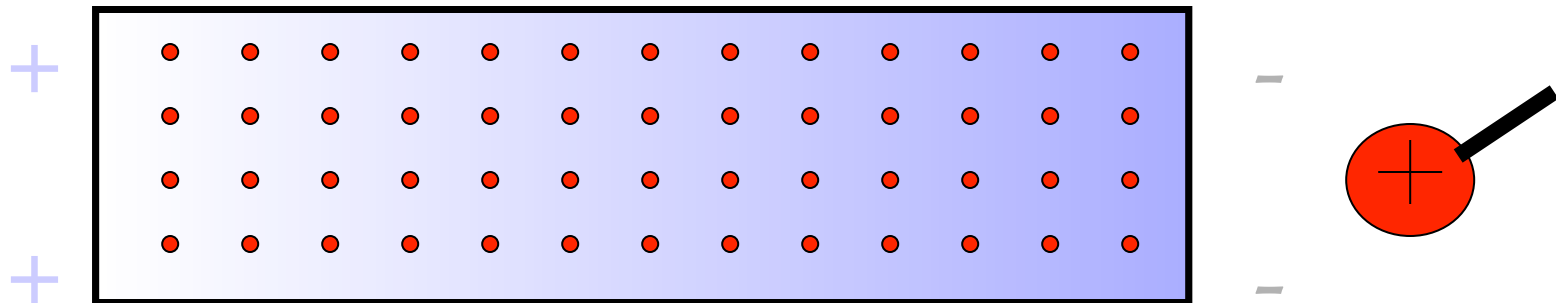


# Charges in solids

- In a **conductor**, electrons move around freely, forming a “sea” of electrons. This is why **metals conduct electricity**.
- Charges can be “induced” (moved around) in conductors.

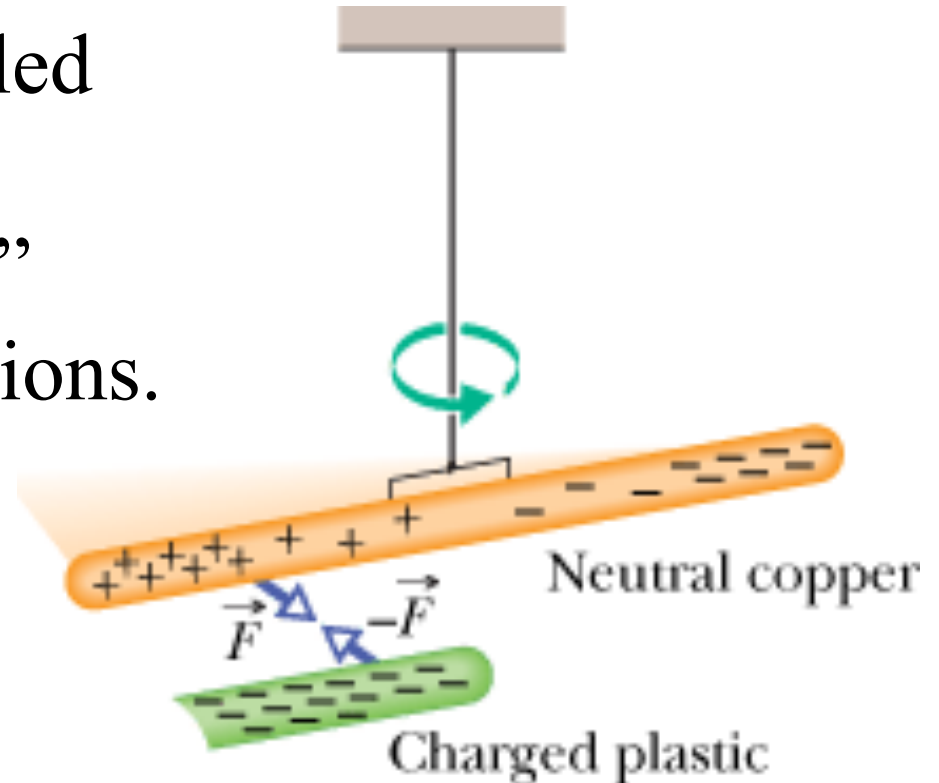
Blue background = mobile electrons

Red circles = static positive charge (nuclei)



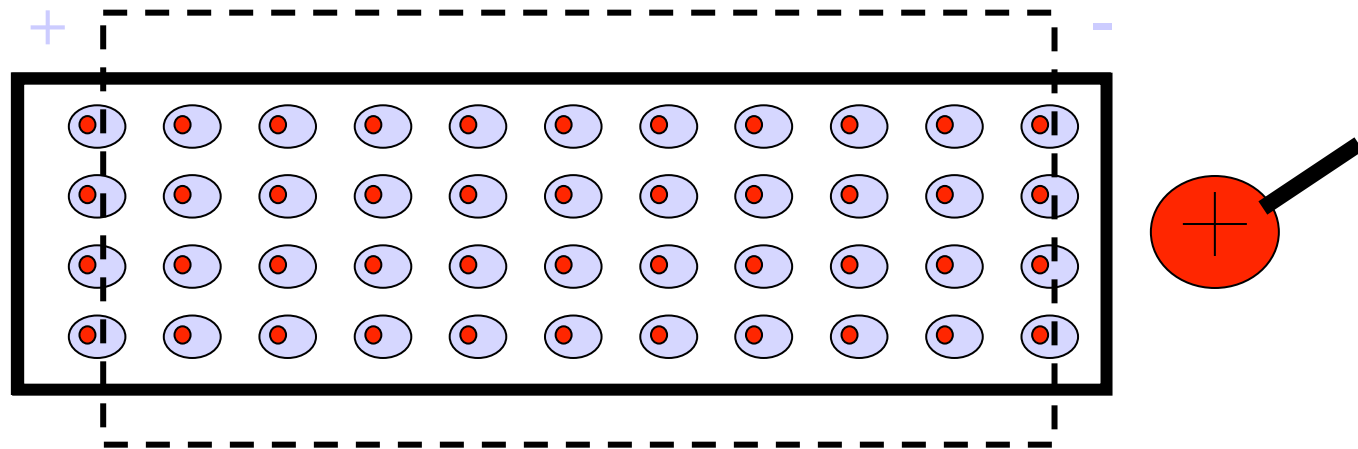
- Since in conductors electrons can move freely (“like water in the sea”), one can alter their distribution just by bringing a charge near the conductor.

- This phenomenon is called “**induction**”. It allows to “move around electricity” without physical connections.



# Insulating solids

- In an **insulator**, each electron cloud is tightly bound to the protons in a nucleus. **Wood, glass, rubber.**
- Note that the electrons are not free to move throughout the lattice, but the electron cloud can “distort” locally.



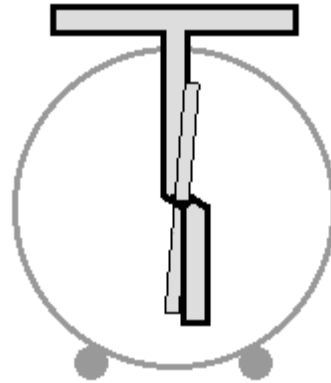
## Materials classified based on their ability to move charge

- **Conductors** are materials in which a significant number of electrons are free to move. Examples include metals.
- The charged particles in nonconductors (**insulators**) are not free to move. Examples include rubber, plastic, glass.
- **Semiconductors** are materials that are intermediate between conductors and insulators; examples include silicon and germanium in computer chips.
- **Superconductors** are materials that are perfect conductors, allowing charge to move without any hindrance.

# How to charge an object

- An object can be given some “excess” charge: giving electrons to it (we give it negative charge) or taking electrons away (we “give” it positive charge).
- How do we do charge an object? Usually, moving charges from one surface to another by adhesion (helped by friction), or by contact with other charged objects.
- If a conductor, the whole electron sea redistributes itself.
- If an insulator, the electrons stay where they are put.
- The amounts of electrons displaced in such macroscopic operations is HUGE, about  $10^9$  to  $10^{10}$  electrons.

# Electroscope



The electroscope is neutral as evidenced by the needle in a relaxed position.



<http://www.physicsclassroom.com/mmedia/estatics/esn.html>



Charles-Augustin  
de Coulomb  
(1736-1806)



# Force between pairs of point charges: Coulomb's law

$$+q_1 \text{ (red circle)} \xrightarrow{F_{12}} \quad F_{21} \xleftarrow{\text{ (blue circle) }} -q_2$$

$$F_{12} \xleftarrow{\text{ (red circle) }} +q_1 \quad +q_2 \text{ (red circle)} \xrightarrow{F_{21}}$$

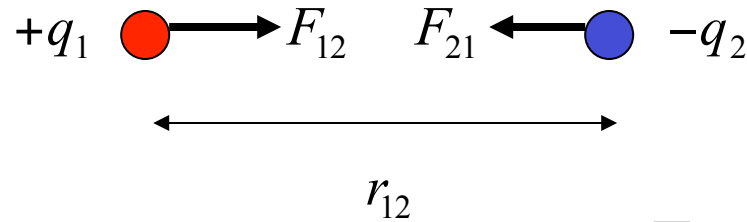
or

$$F_{12} \xleftarrow{\text{ (blue circle) }} -q_1 \quad -q_2 \text{ (blue circle)} \xrightarrow{F_{21}}$$

**Coulomb's law** -- the force between point charges:

- Lies along the line connecting the charges.
- Is proportional to the magnitude of each charge.
- Is inversely proportional to the distance squared.
- Note that Newton's third law says  $|F_{12}| = |F_{21}|!!$

# Coulomb's law



$$|F_{12}| = \frac{k |q_1| |q_2|}{r_{12}^2}$$

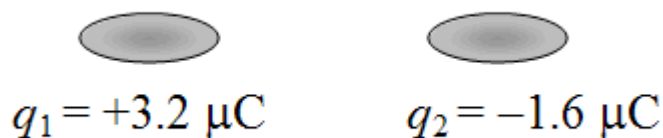
For charges in a  
VACUUM

$$k = 8.99 \times 10^9 \frac{N m^2}{C^2}$$

Often, we write  $k$  as:

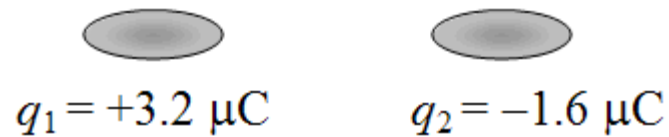
$$k = \frac{1}{4\pi\epsilon_0} \text{ with } \epsilon_0 = 8.85 \times 10^{-12} \frac{C^2}{N m^2}$$

Consider the two charges shown in the drawing. Which of the following statements correctly describes the magnitude of the electric force acting on the two charges?



- a) The force on  $q_1$  has a magnitude that is twice that of the force on  $q_2$ .
- b) The force on  $q_2$  has a magnitude that is twice that of the force on  $q_1$ .
- c) The force on  $q_1$  has the same magnitude as that of the force on  $q_2$ .
- d) The force on  $q_2$  has a magnitude that is four times that of the force on  $q_1$ .
- e) The force on  $q_1$  has a magnitude that is four times that of the force on  $q_2$ .

Consider the two charges shown in the drawing. Which of the following statements correctly describes the direction of the electric force acting on the two charges?



- a) The force on  $q_1$  points to the left and the force on  $q_2$  points to the left.
- b) The force on  $q_1$  points to the right and the force on  $q_2$  points to the left.
- c) The force on  $q_1$  points to the left and the force on  $q_2$  points to the right.
- d) The force on  $q_1$  points to the right and the force on  $q_2$  points to the right.

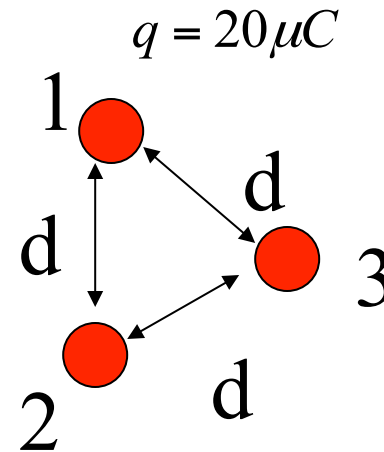
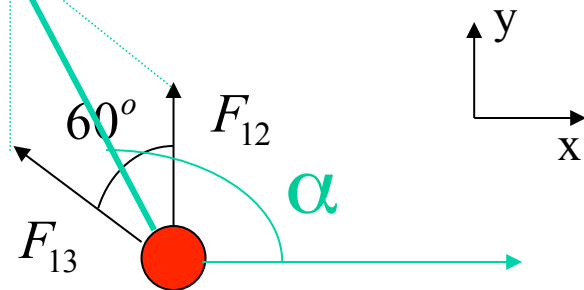
# Superposition

- **Question:** How do we figure out the force on a point charge due to many other point charges?
- **Answer:** consider one pair at a time, calculate the force (a vector!) in each case using Coulomb's Law and finally add all the vectors! (“superposition”)
- Useful to look out for SYMMETRY to simplify calculations!

## Example:

Three equal charges forming an equilateral triangle

Compute force on charge 1



We also know (from previous example) that:  
 $|F_{12}| = |F_{13}| = 1.6N$

And the angle is 60 degrees (equilateral)

Computing x,y components:

$$F_{12}^x = 0,$$

$$F_{12}^y = 1.6N,$$

$$F_{13}^x = 1.6N \sin(60^\circ) = 1.38N,$$

$$F_{13}^y = 1.6N \cos(60^\circ) = 0.8N.$$

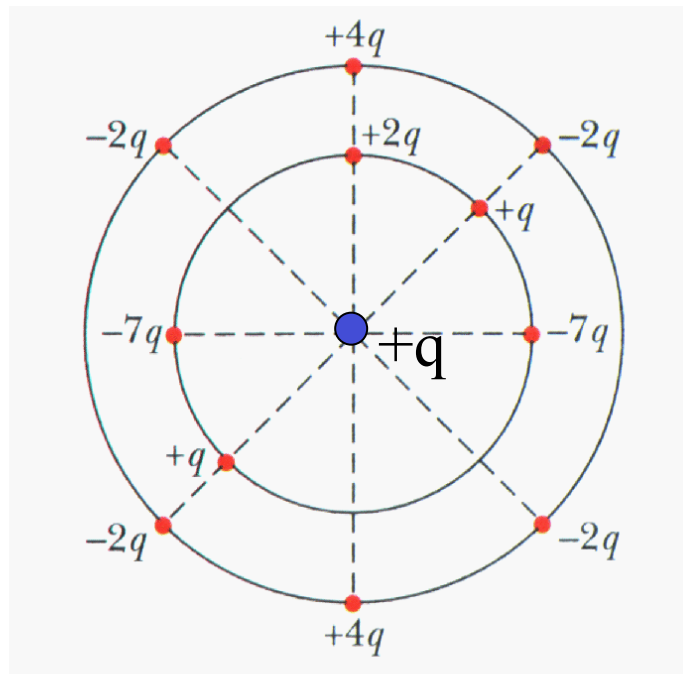
Magnitude of total force:

$$|F_1^{tot}| = \sqrt{(F_1^x)^2 + (F_1^y)^2} = \sqrt{1.38^2 + 2.4^2} N$$

Angle with respect to x axis:

$$\alpha = \arctan\left(\frac{F_1^y}{F_1^x}\right) = \arctan\left(\frac{2.4}{1.38}\right) = 60^\circ \rightarrow 120^\circ$$

# Superposition: symmetry



**Charge  $+q$   
placed at center**

What is the force on central particle?

# Summary

- **Electric charges** come with two signs: **positive and negative**.
- Like charges repel, opposite charges attract, with a magnitude calculated from **Coulomb's law**:  $F = kq_1q_2/r^2$
- Electric forces are added as **vectors**.