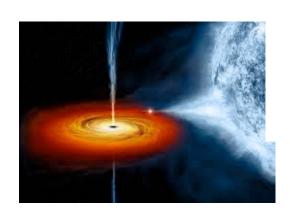


Physics 2113 Lecture 38: MON 1 DEC

CH32: Electromagnetic waves



33-8 Reflection and Refraction 904

33-9 Total Internal Reflection 911

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Reflection and refraction:

Although we saw that generically light from a source spreads out as it gets away from the source, there are many situations in which we can consider light waves as travelling along a straight line. This can be achieved, for instance, by focussing the rays as headlights of cars or flashlights do. The branch of physics that studies this kind of optical phenomena is called geometric optics. It is geometric because as we will see, the laws will refer to the trajectory of the light and will not involve its wave nature.

When light reaches the boundary between two materials, its direction of travel changes. This phenomenon is called refraction.

Incident

Reflected

Experiments show that reflection and refraction keep the outgoing rays in the same plane as the ingoing rays and the normal of the surface and are governed by two laws:

Law of reflection: the angle of incidence θ_1 equals the angle of reflection θ'_1 .

Law of refraction: $n_2 \sin \theta_2 = n_1 \sin \theta_1$ Snell's law.

Where n₁ and n₂ are called the "index of refraction" of media 1 and 2 respectively. These quantities are determined experimentally and listed in tables. For air n is very approximately 1. All other substances have larger indices of refraction.

Wavefront θ_1 θ_1' Air

Interface

Refracted ray

REPUBLIQUE FRANÇAISE θ_2 Republique FRANÇAISE θ_3 θ_4 θ_4 Republique FRANÇAISE

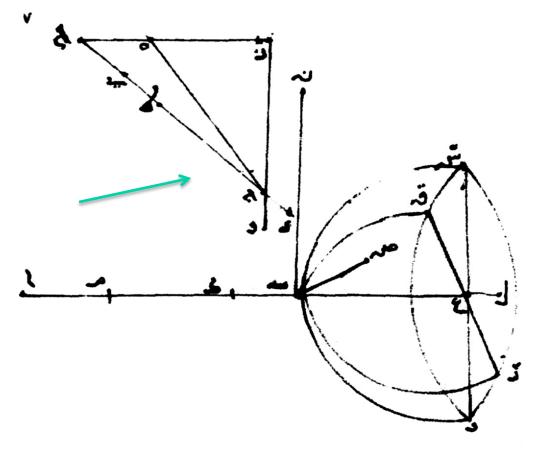
Normal

Incident

Reflected

Willebrord Snell René Descartes 1580-1626 1596-1650

If n_1 equals n_2 then light travels straight. If n_1 is smaller than n_2 then the refracted angle is smaller than the incident, otherwise larger. It can be so large that the light is actually reflected. It can never be so large that it will go beyond the normal.



اندان انده على المعلى المعلى

Ibn Sahl, (Abu Sa`d al-`Ala'ibn Sahl) Baghdad Year 984.

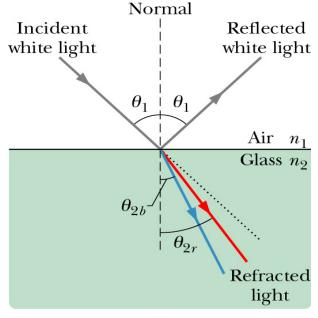
"On burning mirrors and lenses" (Damascus/Tehran Libraries).

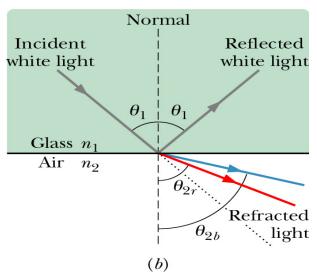
Ibn al-Haytham (Alhazen) 965-1040 popularized an (incorrect) quadratic law due to Ptolemy of Alexandria (circa 150AD), although he knew of Ibn Sahl's results. Europe had the wrong law for over 600 years!

Chromatic dispersion:

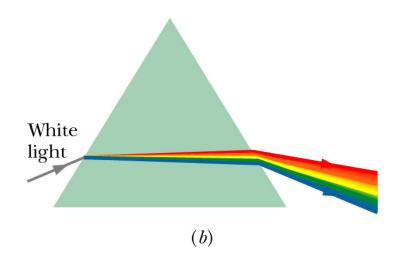
The index of refraction of a medium in general depends on the wavelength of the light. Therefore if one has a beam of light that is composed of waves of more than one frequency, the various waves will refract at different angles.

White light is composed of waves of (nearly) all the frequencies in the visible spectrum. Therefore when white light is refracted, the various components separate.

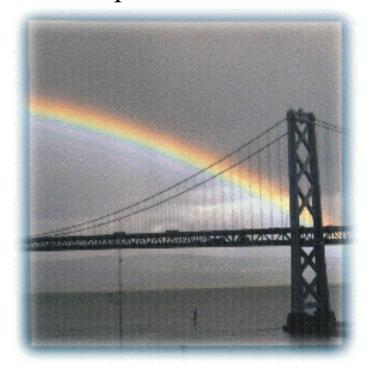


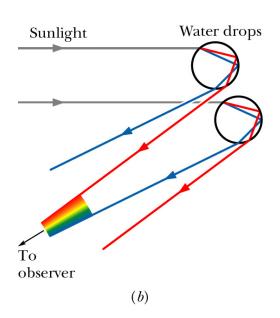


The two previous effects can amplify each other in a prism,



Another example is given by rainbows. Here the water droplets act as "prisms".



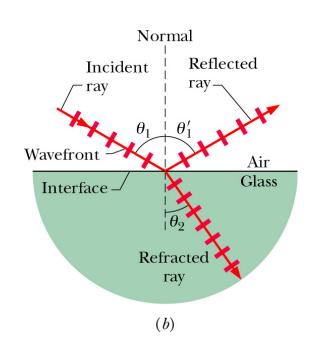


Total internal reflection:

When we discussed the law of refraction:

$$n_2 \sin \theta_2 = n_1 \sin \theta_1$$

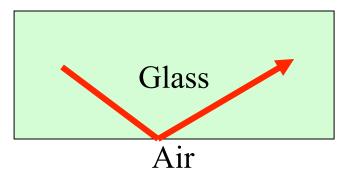
We made clear that it could happen that θ_2 gets bigger than 90°. In such case the ray does not enter the medium at the bottom



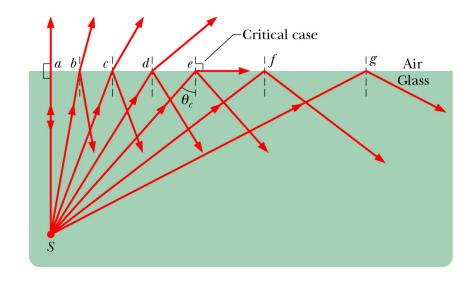
but actually is "reflected" back to the top. Such phenomenon is called "total internal reflection". Why "internal"? For this to happen we

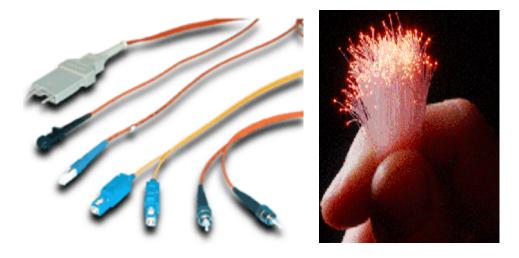
need to at least have,

$$\theta_2 = \frac{\pi}{2} \Rightarrow \sin \theta_1 = \frac{n_2}{n_1}$$



Since sin is always less than one, then $n_2 < n_1$. Therefore this can only happen if the ray comes through a medium of an index of refraction larger into one that is smaller, for instance within glass onto air. The reflection is therefore "internal" in the glass. The angle $\theta_1 = \sin^{-1}(n_2/n_1)$ at which total internal reflection starts to happen is called "critical" angle. For angles of incidence larger than the critical angle light is reflected and not refracted.





This phenomenon has a huge technological application: fiber optics. These are cylinders of flexible material that "guide" light by bouncing it around via total internal reflection. They have had a huge impact in medical imaging (they can be bent into various places) and communications (they are immune to radio interference and many light rays can share a single fiber).

Polarization by reflection:

We argued that one way of polarizing light was through reflection. More precisely, if we decompose the incoming wave into two directions, one perpendicular and one parallel to the plane of incidence, they will be reflected with different amplitudes.

Incident unpolarized ray θ_B Reflected ray θ_B Air n = 1.5 Glass Refracted ray

Light therefore is partially polarized by reflection in general.

Component perpendicular to pageComponent parallel to page

However, when the incident angle has a particular value, called Brewster angle θ_B then the parallel component is not reflected.

It is experimentally observed that at the Brewster angle, the reflected and refracted rays form a straight angle,

$$\theta_R + \theta_R = 90^\circ$$

If we combine the previous observation with Snell's law,

$$n_1 \sin \theta_{\rm B} = n_2 \sin(90^{\circ} - \theta_{\rm B}) = n_2 \cos \theta_{\rm B}$$

$$\tan \theta_{\rm B} = \frac{n_2}{n_1}$$

If we take $n_1=1$, as is the case of air, we get $\theta_B = \tan^{-1} n_2$

$$\theta_{\rm B} = \tan^{-1} n_2$$

Which is known as Brewster's law, and n₂ is the refraction index of a material in air.

Summary:

- Light rays deviate when entering a medium. Refraction is governed by Snell's law.
- The deviation can be such that the ray is reflected.
- Light rays are polarized by reflection, this is governed by Brewster's law.